

Graph Transformation-based Stochastic Simulation

Paolo Torrini

joint work with Reiko Heckel and Ajab Khan

pt95@mcs.le.ac.uk

University of Leicester

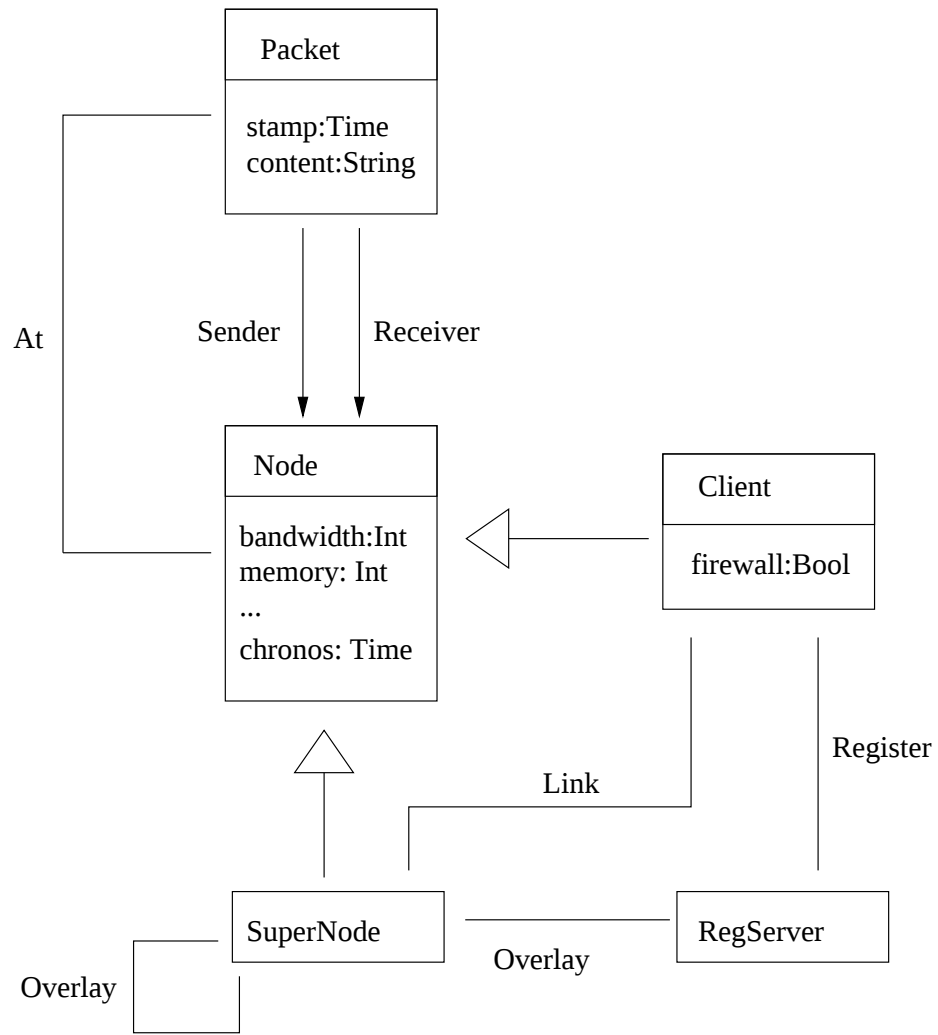
Network reconfiguration

- Graph Transformation Systems as modelling technique
- Stochastic simulation as validation technique
- Application: simulation of system reconfiguration and behaviour
- Present focus: reconfiguration of P2P networks (previous work by Reiko), VoIP applications — esp. Skype (Ajab's PhD)
- Semantics: stochastic GTS interpreted as stochastic processes (previous work by Reiko *et al.*)
- Implementation: based on existing GTS tools (VIATRA)

Modelling networks

- Network as a typed graph (SPO):
components as nodes
connections as edges
- Transformations in our model:
basic behaviour
 - sending packets
 - checking QoS parameters
 - connection/disconnection of clientsreconfiguration
 - change of node status, client-supernode and overlay connections to improve QoS

Type graph



Stochastic approach

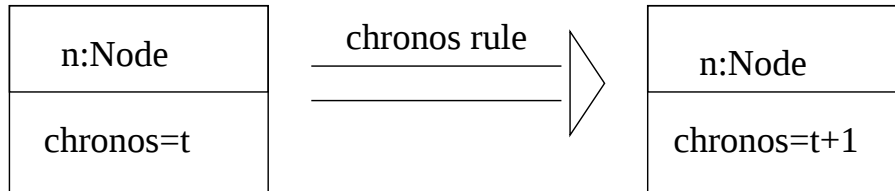
- Probabilistic rather than indeterministic actions
- Simulation based on sampling delay values according to given distributions
- Individual processes determined by Random Number Generator
- Rule application associated with an expected delay according to a probability distribution function

Probability distributions

- Expected delay (timer) — random variable associated to probability distribution function
- $F_T(x) = P\{T \leq x\}$
- Exponential distribution — determined by a rate, depends only on the present state
- Normal distribution — determined by mean and variance, finer modelling

Representing time

- Each component has a clock — *chronos* attribute
- *chronos* rule to advance time
- Normally distributed
— exponential distribution would not do



GTS with probability

- Stochastic Graph Transformation Systems:
rules associated with exponential probability distributions
- Generalised Stochastic Graph Transformation Systems:
rule matches associated with general probability distributions
- Rule matches as equivalence classes to preserve inter-graph identity
— restrictions on GSGTS to ensure they are a proper set (numbered graphs)
- Continuous time — timers are independent variables, so probability of two actions taking place at the same time is 0. So we skip parallelism

Stochastic processes

- Continuous-time stochastic process — time-indexed family of random variables over states
- Markov process: next state depends on current state only, interevent time is exponentially distributed
- Semi-Markov process: next state depends on time spent in current state, too
- Translation of GSGTS to Generalised Semi-Markov Processes

Stochastic structures

- Generalised Semi-Markov process:
generated by a structure based on timers + race condition
- Timers as stochastic clock structure: Stochastic Timed Automata
- Timers set by RNG: Generalised Semi-Markov Scheme
- Timers do not need to be reset at each state change
i.e. they do not need to be exponential — so neither interevent time do

GSGTS

- SPO — components may disconnect without warning
- $\mathcal{G} = \langle TG, P, \pi, G_0, F \rangle$
- Type graph, rule names, initial graph
- F maps rule matches to probability distribution functions (cumulative distributions:
— max delay value mapped to probability)

GSMS

$$\begin{aligned} \mathcal{P} = \langle & \textit{States} \\ & \textit{Events} \\ & \textit{ActiveStates} : \textit{State} \rightarrow \wp \textit{Event} \\ & \textit{Transition} : \textit{State} \times \textit{Event} \rightarrow \textit{State} \\ & \Delta : \textit{Event} \rightarrow (\mathcal{R} \rightarrow [1, 0]) \\ & \textit{InitialState} : \textit{State} \quad \rangle \end{aligned}$$

from GSGTS to GSMS

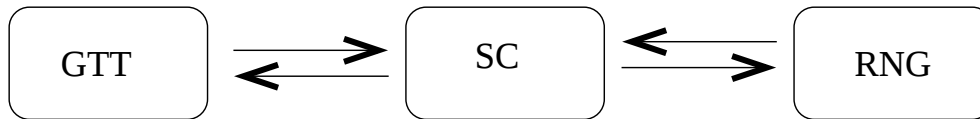
$$\begin{aligned} \mathcal{P} = \langle & \textit{ReachGraphs} \\ & \textit{RuleMatches} \quad (\text{equivalence classes}) \\ & \textit{EnabledMatches} : \textit{ReachGraph} \rightarrow \wp \textit{RuleMatch} \\ & \textit{GraphTrans} : \\ & \quad \textit{ReachGraph} \times \textit{RuleMatch} \rightarrow \textit{ReachGraph} \\ & F : \textit{RuleMatch} \rightarrow (\mathcal{R} \rightarrow [1, 0]) \\ & \textit{InitialGraph} : \textit{ReachGraph} \quad \rangle \end{aligned}$$

GSMS-based simulation

- Simulation of GSMP based on Event Scheduling Scheme algorithm
- Refinement of ESS
 - for GSMP obtained from GSGTS
- Substantial problem: computation of active matches
 - we need to keep track of pre-existing matches
- Incremental pattern-matching
 - implemented in VIATRA (Eclipse plug-in)
- Planned Java implementation using SSJ libraries for RNG

Implementation architecture

- Graph transformation tool (GTT)
- Simulation control (SC)
- Random number generator (RNG)



Scheduling Scheme I

- Initial input:
 - graph transformation system (for GTT)
 - simulation time t (for SC)
 - probability distribution functions (for RNG)
- Initialisation:
 - active matches of the initial graph computed by GTT
 - associated to scheduled delay d (from RNG)
 - scheduled time = $t + d$
 - collected in list ordered by scheduled time
- list ordering implements race condition

Simulation Control

1. First item $(\langle r, m \rangle, t')$ removed from list, simulation time updated to t'
2. Graph update (by GTT)
 - rule r applied to the current graph at m
 - new and surviving matches are computed (incremental approach should help)
3. New matches are associated to scheduling times
 - RNG calls
4. list ordering

Further work

- Containment relations and spatial aspect — to model domains, firewall restrictions, geographic locations
- *Chronos* rule application overkill: two possible strategies
 - temporal granularity with laziness
 - synchronous approach (global time)
- Comparison with existing simulation tools (such as NS2)
- A. Kahn, P. Torrini, R. Heckel — *Model-based Simulation of VoIP Network Reconfigurations using Graph Transformation Systems*
Doctoral Symposium ICGT 2008 (post-proceedings, 2009)