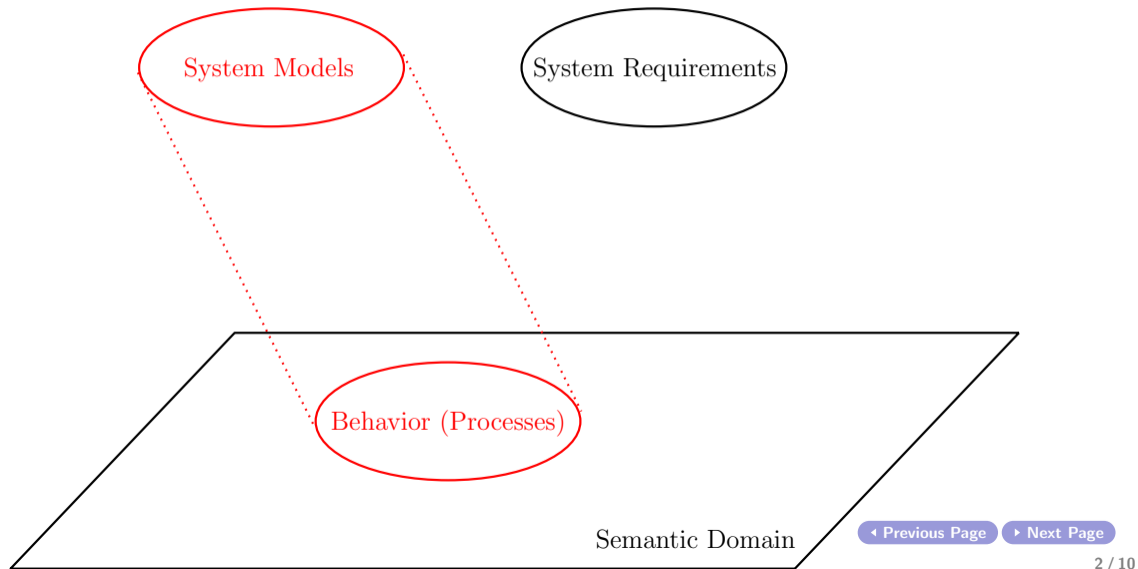


Formal Modelling and Analysis of Concurrent Systems: Actions, Behaviour and Abstraction

Mohammad Mousavi and Jeroen Keiren

General Overview



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Actions

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- ▶ Action can happen **internally** in a system, or **externally** with the environment
- ▶ Depends on level of **abstraction**
- ▶ Actions can be **composed** to obtain **behaviour**

Actions: An Example

What (inter)actions does a coffee machine have?



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- ▶ coffee, tea, coin



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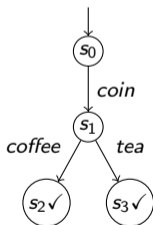
- ▶ coffee, tea, coin
- ▶ grind



Composing Actions Into Behaviour

- ▶ Actions alone do not describe the behaviour of a system!
- ▶ We need to add **structure** and **dependencies**

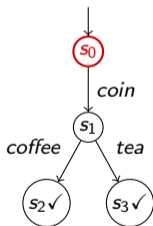
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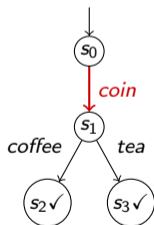
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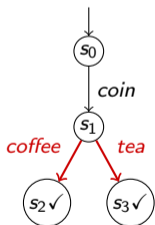
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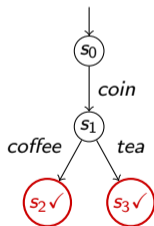
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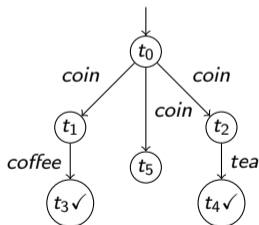
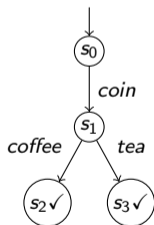
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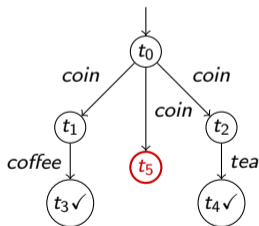
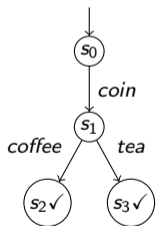
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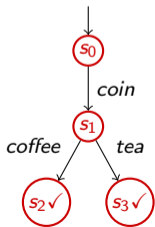
Labelled Transition Systems

An LTS is a 5-tuple $\langle S, Act, \rightarrow, s, T \rangle$:

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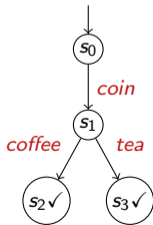


- ▶ $S = \{s_0, s_1, s_2, s_3\}$

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An LTS is a 5-tuple $\langle S, Act, \rightarrow, s, T \rangle$:

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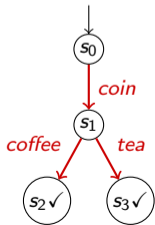
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Labelled Transition Systems

An LTS is a 5-tuple $\langle S, Act, \rightarrow, s, T \rangle$:

- ▶ S is a set of *states*
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- ▶ $\rightarrow \subseteq S \times Act \times S$ is the *transition relation*

Write $t \xrightarrow{a} t'$ for $(t, a, t') \in \rightarrow$



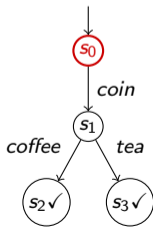
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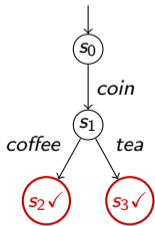
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- ▶ $s \in S$ is the *initial state*
- ▶ $T \subseteq S$ is the set of *terminating states*

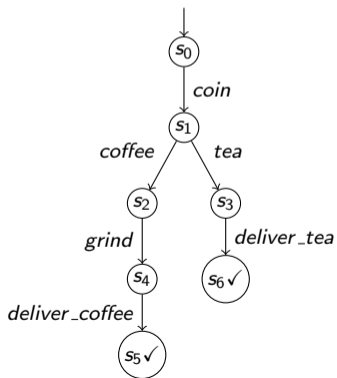
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- ▶ $s = s_0$
- ▶ $T = \{s_2, s_3\}$

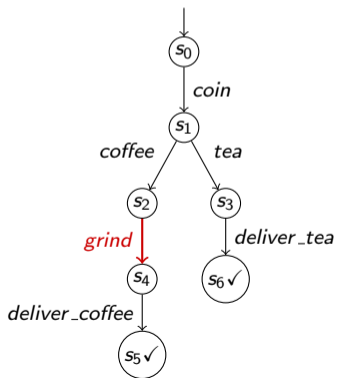
Internal Behaviour

- ▶ Some behaviour is **internal** to the system



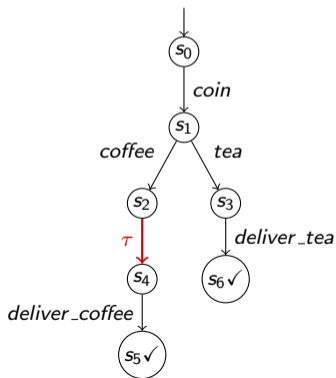
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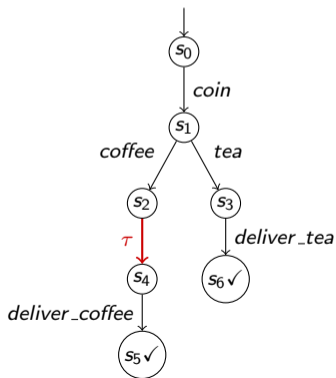
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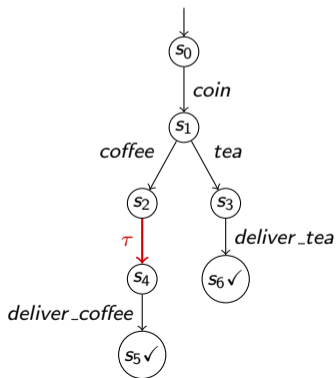
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- ▶ **Abstract** from it using **internal action**
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- ▶ $Act_{\tau} = Act \cup \{\tau\}$



Summary

- ▶ **Actions** main building block
- ▶ **Behaviour** described as **Labelled Transition System**
- ▶ **Abstraction** of **internal** actions: τ

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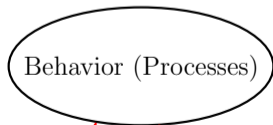
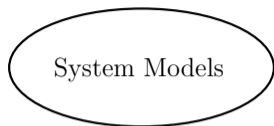
Behavior (Processes)

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Behavioral Equivalences

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Thank you very much.